

CORRELATION ANALYSIS OF STABILITY CONSTANTS OF COMPLEXES
FORMED BETWEEN ALKALI METAL CATIONS AND MACROCYCLES

Bo-Long Poh

School of Chemical Sciences, Universiti Sains Malaysia, Penang, Malaysia

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Abstract: The stability constants K_a of 1:1 complexes formed between alkali metal cations and macrocycles are correlated by the equation $\log K_a = m|R_c - R_m| + b$ where R_c and R_m are the radii of the macrocycle cavity and the alkali metal cations respectively, m and b are constants for a given macrocycle.

Introduction. Complexation between alkali metal cations and synthetic macrocycles have been extensively investigated. The stability constants K_a of many such complexes (usually of 1:1 host to guest stoichiometry) have been determined.¹ The $\log K_a$ values are usually plotted against the radii R_m of the alkali metal cations. The plots are usually curve shaped, with a maximum at a radius equalling to the radius R_c of the macrocycle cavity. Such plots are of little use for correlating stability constants. In this paper, a better and more useful method of correlating the $\log K_a$ data is presented.

Method. Two assumptions (justified by the good correlation results shown later) are made concerning the formation of 1:1 complexes between the alkali metal cations and a given macrocycle. First, the macrocycle maintains the same cavity size in complexing with the different alkali metal cations. Second, two metal cations, one larger and the other smaller, than the macrocycle cavity by the same amount (that is, same $|R_c - R_m|$ absolute value) give complexes of equal stability. These two assumptions lead to the following equation

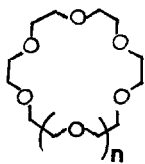
$$\log K_a = m|R_c - R_m| + b \quad (1)$$

where m and b are constants for a given macrocycle host.

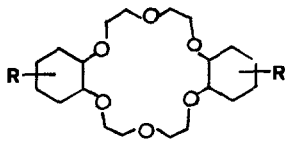
Since the exact value of R_c is not known, R_c is varied until the best correlation between $\log K_a$ and $|R_c - R_m|$ is obtained.

Results and Discussion. The $\log K_a$ values of 116 complexation equilibria involving 104 macrocycles were correlated using equation 1. A summary of the correlation results is given in Table I and the details of the correlations in Table II. Table III and IV contain the R_m and $\log K_a$ values used in the correlations. Some representative plots are shown in Figure 1.

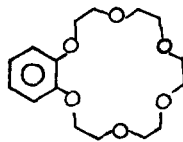
Macrocycles used in the correlations



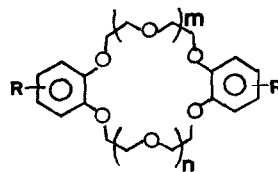
A1 $n=0$
 A2 $n=1$
 A3 $n=2$



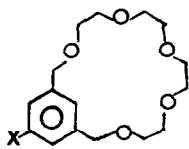
A4 $R=H$
 A5 $R=Bu^t$



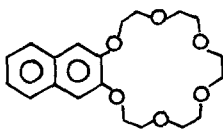
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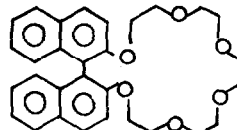
A7 $m,n=1, R=H$
 A8 $m,n=3, R=H$
 A9 $m,n=3, R=Me$



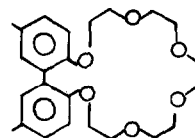
A10 $X=H$
 A11 $X=Br$
 A12 $X=Bu^t$
 A13 $X=OMe$
 A14 $X=CN$



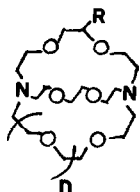
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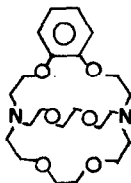
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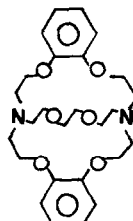
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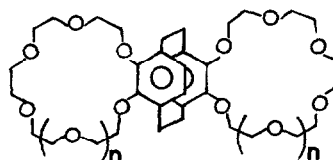
A18 $n=0, R=H$
 A19 $n=1, R=H$
 A20 $n=1, R=C_{10}H_{23}$



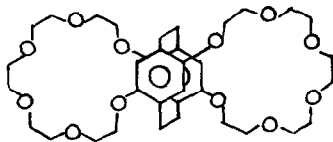
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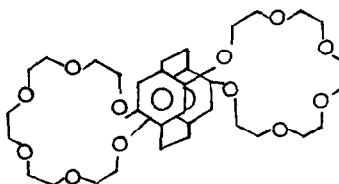
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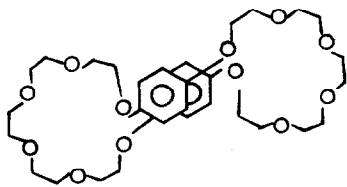
A23 $n=0$
 A24 $n=1$



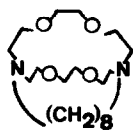
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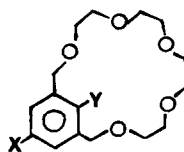
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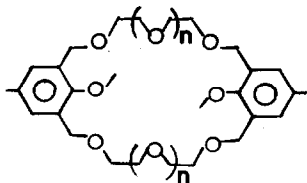
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A28

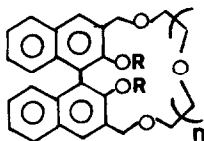
B1 X=H, Y=CO₂Me

B2 X=Me, Y=OMe



B3 n=0

B4 n=1



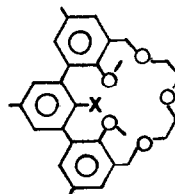
B5 n=2, R=Me

B6 n=3, R=Me

B7 n=2, R=H

B8 n=3, R=H

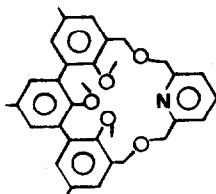
B9 n=4, R=H



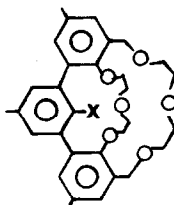
B10 X=OMe

B11 X=OCH₂CHCH₂

B12 X=OH

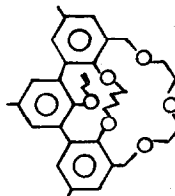


B13

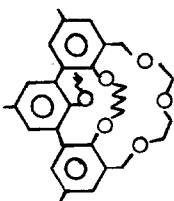
B14 X=OCH₂CHCH₂

B15 X=OH

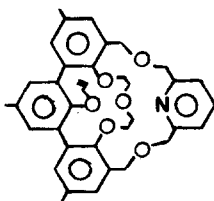
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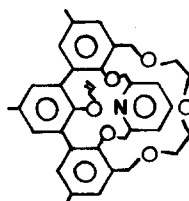
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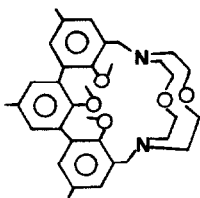
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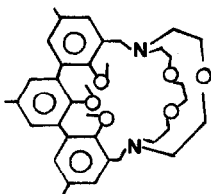
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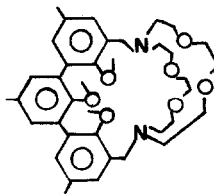
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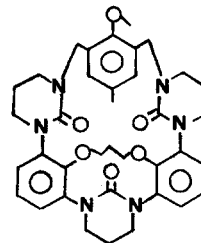
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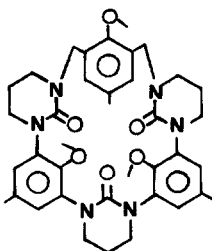
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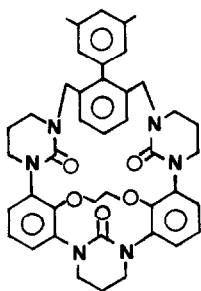
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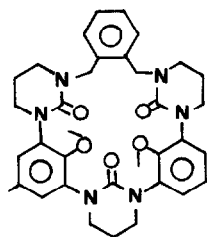
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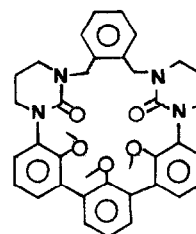
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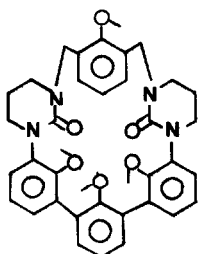
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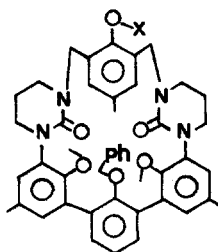
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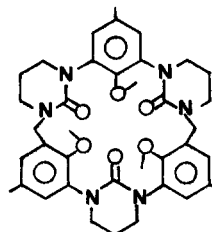
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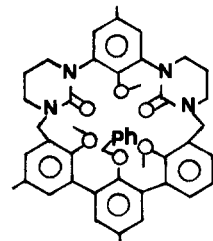
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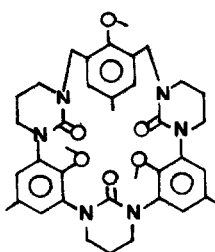
B30 X=H

B31 X=CH₂CHCH₂

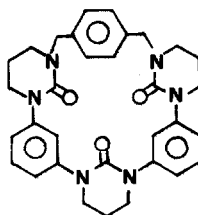
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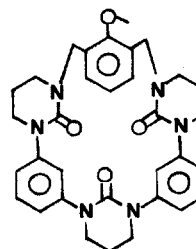
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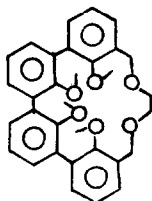
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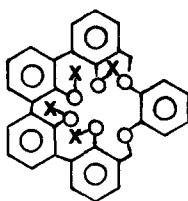
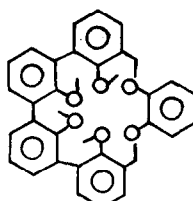
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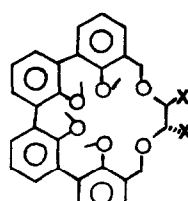
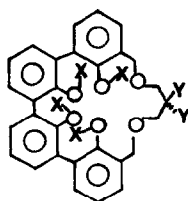
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B37

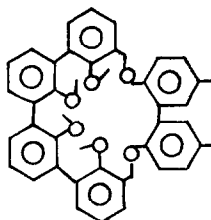
B38 X=Me
B39 X=Et

B40

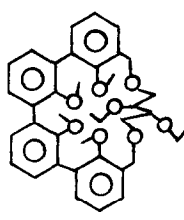
B41 X=CH₂OCH₂Ph

B42 X=Me, Y=H

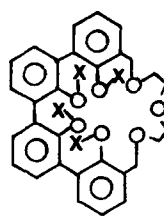
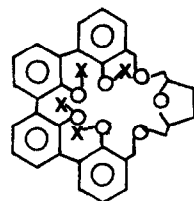
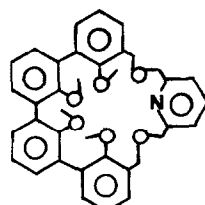
B43 X=Et, Y=H

B44 X=Me, Y=CH₂OMe

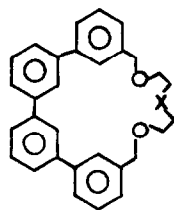
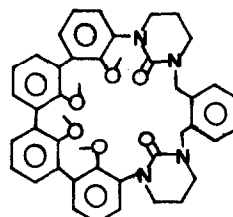
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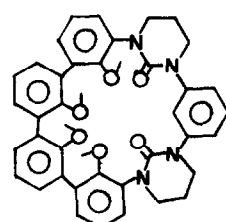
B46

B47 X=Me
B48 X=EtB49 X=Me
B50 X=Et

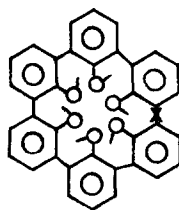
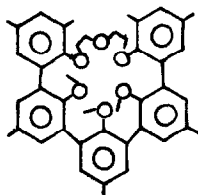
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B52 X=S
B53 X=SO
B54 X=SO₂

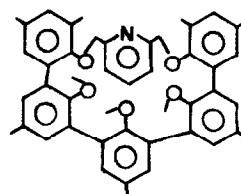
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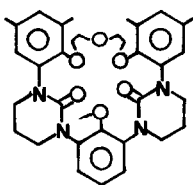
B56

B57 X=CH₂CH₂
B58 X=CH₂SCH₂
B59 X=CH₂SO₂CH₂

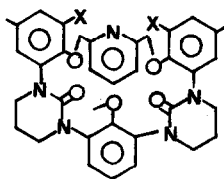
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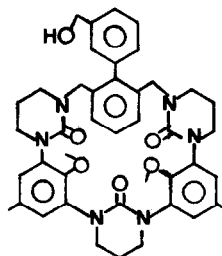
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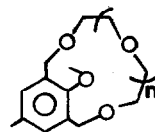
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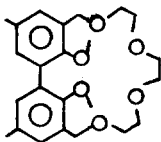
B63 X=Me
B64 X=CH₂OMe



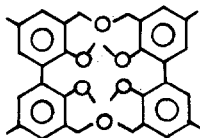
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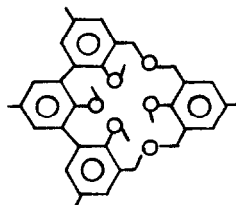
B66 n=2
B67 n=4



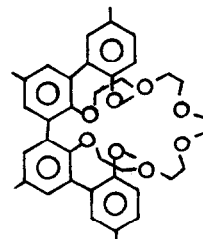
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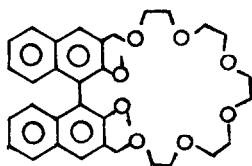
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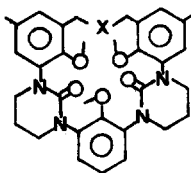
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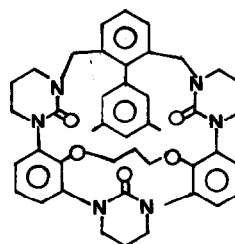
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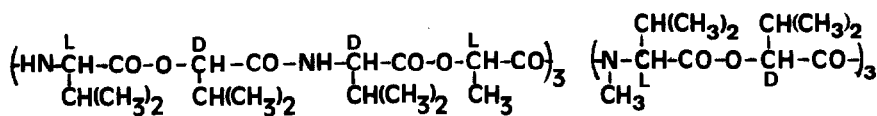
B72



B73 X=O
B74 X=S
B75 X=C(CO₂Et)₂
B76 X=1,2-C₆H₄O₂

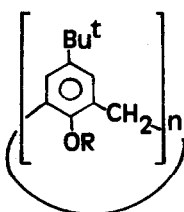


B77



B78

B79



C1 n=4, R=CH₂CO₂Et
C2 n=4, R=CH₂COMe
C3 n=4, R=CH₂COBu^t
C4 n=4, R=CH₂COPh
C5 n=6, R=CH₂CO₂Et

Table I. Summary of Correlation Analysis Results

Compounds	Correlation coefficient				Confidence level (%)		
	$r \geq 0.99$	$0.95 \leq r \leq 0.99$	$0.90 \leq r < 0.95$	$r < 0.90$	≥ 99	95 to 99	< 95
A series	18	17	5	0	31	9	0
B series	15	43	12	6	59	15	2

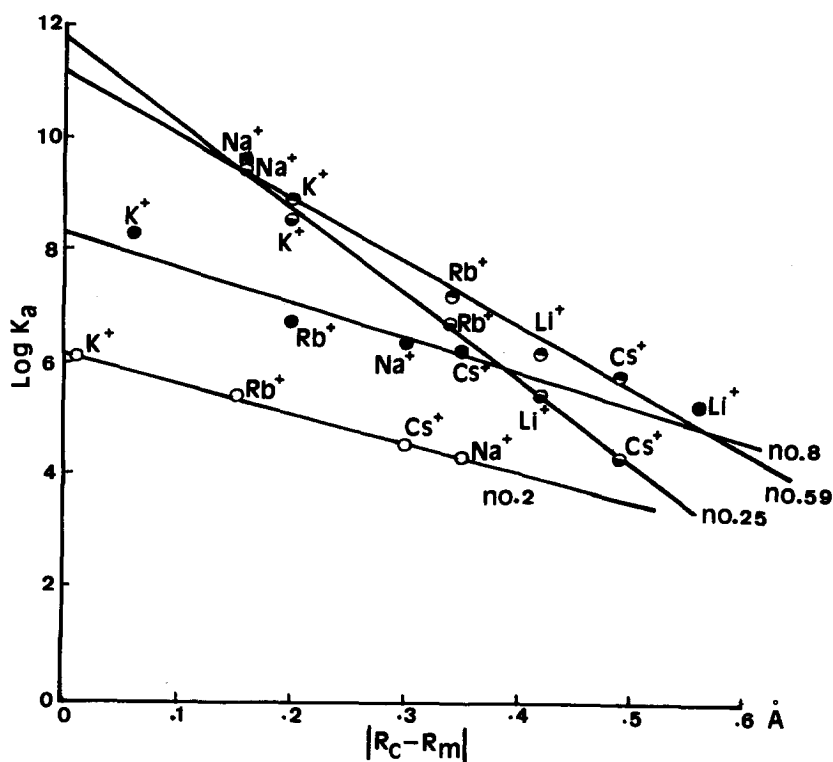


Figure 1. Linear relationship of stability constants of complexes formed between alkali metal cations and macrocycles

Table II. Correlations of Stability Constants^a of 1:1 Complexes Formed between Alkali Metal Cations and Macrocycles at 25°C

No.	Host	Solvent	R _c (A)	n ^b	r ^c	m	b	sd ^d	cl(X) ^e
1	A1	MeOH	1.25	4	0.943	-6.07	4.50	0.31	97.0
2	A2	MeOH	1.37	4	0.999	-5.12	6.15	0.02	99.95
3	A2	H ₂ O	1.37	4	1.000	-3.63	2.08	0.01	>99.95
4	A2	70% MeOH	1.35	4	0.995	-5.09	4.43	0.06	99.8
5	A2	PC ^f	1.26	4	0.997	-6.11	6.96	0.05	99.8
6	A3	MeOH	1.60	4	0.997	-5.58	5.40	0.09	99.8
7	A4 ^g	H ₂ O	1.34	5	0.994	-2.56	2.06	0.05	>99.95
8	A4	CDCl ₃	1.32	5	0.958	-5.67	8.25	0.28	99.5
9	A5	H ₂ O	1.31	4	0.974	-3.79	2.36	0.10	98.5
10	A6	MeOH	1.30	4	0.989	-6.54	6.24	0.07	99.4
11	A6	PC ^f	1.21	4	1.000	-6.26	6.47	0.00	>99.95
12	A6	MeCN	1.23	4	0.992	-5.12	5.99	0.09	99.6
13	A6	MeCN ^h	1.23	4	0.967	-6.57	6.51	0.12	98.1
14	A7	MeOH	1.26	4	0.998	-5.00	5.58	0.03	99.9
15	A8	MeOH	1.48	4	0.979	-6.33	5.12	0.21	98.9
16	A9	MeCN ⁱ	1.42	4	0.941	-3.91	5.05	0.20	96.8
17	A10	CDCl ₃	1.47	5	0.987	-4.65	5.35	0.19	99.9
18	A11	CDCl ₃	1.45	5	0.987	-3.98	4.79	0.16	99.9
19	A12	CDCl ₃	1.47	5	0.984	-4.16	5.28	0.20	99.8
20	A13	CDCl ₃	1.46	5	0.984	-3.96	5.33	0.17	99.8
21	A14	CDCl ₃	1.38	5	0.970	-1.77	4.01	0.09	99.7
22	A15	CDCl ₃	1.35	5	1.000	-6.40	8.13	0.03	>99.95
23	A16	CDCl ₃	1.29	5	0.929	-6.12	7.92	0.39	98.8
24	A17	CDCl ₃	1.28	5	0.976	-4.37	6.47	0.12	99.8
25	A18	MeOH	1.18	5	0.998	-15.2	11.8	0.12	>99.95
26	A18	PC ^f	1.07	5	0.991	-14.9	13.9	0.39	>99.95
27	A18	MeCN	1.17	4	0.986	-17.8	13.8	0.41	99.9
28	A18	CDCl ₃	1.17	4	0.986	-19.9	15.8	0.43	99.2

Table II. cont.

No.	Host	Solvent	R_c (Å)	n^b	r^c	a	b	sd^d	cl(%) ^e
29	A19	MeOH	1.27	5	0.985	-21.1	13.3	0.51	99.9
30	A19	H ₂ O	1.25	5	0.984	-12.0	6.91	0.28	99.9
31	A19	CDCl ₃	1.30	4	0.997	-30.1	18.8	0.16	99.8
32	A20	MeOH	1.26	5	0.987	-20.6	12.1	0.29	99.9
33	A21	MeOH	1.24	5	0.990	-21.3	12.4	0.38	99.5
34	A22	MeOH	1.23	5	1.000	-20.7	11.8	0.08	>99.95
35	A23	CDCl ₃	1.17	5	0.912	-5.30	6.66	0.31	98.2
36	A24	CDCl ₃	1.38	4	0.993	-4.97	7.12	0.13	99.6
37	A25	CDCl ₃	1.51	5	0.991	-2.36	5.17	0.09	99.95
38	A26	CDCl ₃	1.38	5	0.992	-3.99	5.98	0.10	>99.95
39	A27	CDCl ₃	1.45	4	0.937	-1.83	4.18	0.10	98.2
40	A28	MeOH ^j	1.29	4	0.964	-8.54	5.77	0.24	97.8
41	B1	CDCl ₃	1.30	4	0.946	-5.09	7.25	0.23	97.2
42	B2	CDCl ₃	1.38	4	0.990	-3.69	6.17	0.12	99.5
43	B3	CDCl ₃	1.33	5	0.989	-1.22	3.65	0.03	99.9
44	B4	CDCl ₃	1.30	5	0.900	-3.00	4.54	0.19	98.0
45	B5	CDCl ₃	1.30	4	0.980	-6.55	7.90	0.17	99.0
46	B6	CDCl ₃	1.58	5	0.985	-2.68	6.27	0.14	99.9
47	B7	CDCl ₃	1.46	4	0.999	-2.08	4.80	0.02	99.95
48	B8	CDCl ₃	1.56	5	0.978	-2.21	5.55	0.14	99.8
49	B9	CDCl ₃	k	5	0.963	1.66	2.60	0.15	99.6
50	B10	CDCl ₃	1.23	5	0.944	-10.7	10.7	0.47	99.2
51	B11	CDCl ₃	1.21	5	0.973	-11.4	10.6	0.34	99.7
52	B12	CDCl ₃	1.20	5	0.963	-3.78	6.45	0.13	99.6
53	B13	CDCl ₃	1.19	5	0.966	-10.1	10.1	0.34	99.6
54	B14	CDCl ₃	1.24	5	0.984	-11.7	11.4	0.26	99.8
55	B15	CDCl ₃	1.25	5	0.987	-6.66	8.15	0.14	99.9
56	B16	CDCl ₃	1.26	5	0.986	-12.6	12.0	0.29	99.9

Table II. cont.

No.	Host	Solvent	R_c (A)	n^b	r^c	m	b	sd^d	ct (%) ^e
57	B17	$CDCl_3$	1.17	5	0.950	-9.80	8.62	0.42	99.3
58	B18	$CDCl_3$	1.21	5	0.984	-8.42	7.95	0.19	99.9
59	B19	$CDCl_3$	1.18	5	0.994	-11.5	11.2	0.16	>99.95
60	B20	$CDCl_3$	1.22	5	0.986	-9.73	12.4	0.21	99.9
61	B21	$CDCl_3$	0.95	5	0.999	-11.3	15.9	0.14	>99.95
62	B22	$CDCl_3$	1.26	4	0.999	-21.2	20.5	0.12	99.95
63	B23	$CDCl_3$	k	5	0.996	9.77	-0.02	0.28	>99.95
64	B24	$CDCl_3$	1.01	5	0.996	-1.27	9.43	0.02	>99.95
65	B25	$CDCl_3$	1.23	5	0.981	-7.69	12.71	0.19	99.8
66	B26	$CDCl_3$	1.16	5	0.955	-6.74	11.28	0.28	99.3
67	B27	$CDCl_3$	0.76	5	0.973	-5.89	13.3	0.46	99.7
68	B28	$CDCl_3$	0.79	5	0.950	-6.35	12.3	0.49	99.3
69	B29	$CDCl_3$	1.20	5	0.981	-8.34	12.3	0.20	99.8
70	B30	$CDCl_3$	1.17	5	0.915	-7.74	12.8	0.44	98.3
71	B31	$CDCl_3$	1.18	5	0.944	-6.20	10.2	0.27	99.2
72	B32	$CDCl_3$	1.16	5	0.960	-9.77	9.87	0.37	99.5
73	B33	$CDCl_3$	1.13	5	0.910	-9.07	12.1	0.59	98.3
74	B34	$CDCl_3$	1.23	5	0.972	-7.33	12.5	0.22	99.7
75	B35	$CDCl_3$	k	5	0.956	1.67	2.92	0.17	99.4
76	B36	$CDCl_3$	1.31	5	0.992	-3.71	7.49	0.08	>99.95
77	B37	$CDCl_3$	1.16	5	0.952	-12.9	11.1	0.54	99.3
78	B38	$CDCl_3$	1.19	5	0.923	-11.5	10.8	0.60	98.6
79	B39	$CDCl_3$	1.22	5	0.937	-10.9	10.8	0.50	99.0
80	B40	$CDCl_3$	1.13	5	0.898	-6.46	7.18	0.46	97.9
81	B41	$CDCl_3$	1.20	5	0.923	-11.5	10.3	0.59	98.6
82	B42	$CDCl_3$	1.16	5	0.715	-2.64	5.84	0.34	91.4
83	B43	$CDCl_3$	1.38	5	0.932	-0.97	4.61	0.08	98.9
84	B44	$CDCl_3$	1.25	5	0.972	-5.09	6.65	0.16	99.7

Table II. cont.

No.	Host	Solvent	R_c (Å)	n^b	r^c	m	b	sd^d	cl(%) ^e
85	B45	CDCl ₃	1.30	5	0.994	-8.84	9.65	0.12	>99.95
86	B46	CDCl ₃	1.38	5	0.991	-3.36	6.36	0.09	99.95
87	B47	CDCl ₃	1.48	5	0.972	-5.95	8.82	0.32	99.7
88	B48	CDCl ₃	1.57	5	0.975	-4.86	8.38	0.33	99.8
89	B49	CDCl ₃	1.46	5	0.968	-4.22	9.07	0.27	99.6
90	B50	CDCl ₃	1.48	5	0.965	-6.07	8.72	0.42	99.6
91	B51	CDCl ₃	1.55	5	0.998	-2.67	7.41	0.05	>99.95
92	B52	CDCl ₃	1.46	5	0.978	-3.92	6.99	0.37	99.8
93	B53	CDCl ₃	1.30	5	0.977	-4.27	6.91	0.18	99.8
94	B54	CDCl ₃	1.30	5	0.981	-7.27	7.97	0.19	99.8
95	B55	CDCl ₃	1.19	5	0.989	-8.80	9.28	0.17	99.9
96	B56	CDCl ₃	1.45	5	0.953	-2.14	6.11	0.16	99.3
97	B57	CDCl ₃	1.21	5	0.998	-12.2	9.59	0.10	99.95
98	B58	CDCl ₃	1.32	4	0.985	-7.05	7.94	0.14	99.2
99	B59	CDCl ₃	1.25	5	0.997	-9.50	8.66	0.09	99.95
100	B60	CDCl ₃	1.26	5	0.968	-7.53	10.1	0.26	99.6
101	B61	CDCl ₃	1.22	5	0.855	-8.28	10.8	0.62	96.5
102	B62	CDCl ₃	1.30	5	0.960	-7.28	9.04	0.27	99.5
103	B63	CDCl ₃	1.20	5	0.927	-4.83	7.87	0.24	98.7
104	B64	CDCl ₃	1.21	5	0.926	-4.91	8.56	0.25	98.7
105	B65	CDCl ₃	1.19	5	0.966	-8.63	12.6	0.29	99.6
106	B66	CDCl ₃	1.26	4	1.000	-2.17	4.63	0.04	>99.95
107	B67	CDCl ₃	1.60	4	0.978	-2.83	6.01	0.18	98.8
108	B68	CDCl ₃	1.31	5	0.979	-4.97	7.54	0.16	99.8
109	B69	CDCl ₃	1.07	4	0.973	-1.84	3.88	0.09	98.4
110	B70	CDCl ₃	1.20	5	0.846	-6.42	6.30	0.49	96.2
111	B71	CDCl ₃	1.23	5	0.976	-10.3	9.81	0.29	99.8
112	B72	CDCl ₃	1.63	5	0.983	-1.73	5.62	0.11	99.8

Table II. cont.

No.	Host	Solvent	R_c (Å)	n^b	r^c	m	b	sd^d	cl(%) ^e
113	B73	CDCl ₃	1.02	5	0.993	-5.60	14.2	0.15	99.95
114	B74	CDCl ₃	1.02	5	0.972	-8.31	13.7	0.45	99.7
115	B75	CDCl ₃	0.82	5	0.983	-5.57	12.1	0.31	99.8
116	B76	CDCl ₃	0.83	5	0.745	1.51	7.51	0.40	92.0
117	B77	CDCl ₃	1.19	5	0.883	-5.51	12.7	0.37	97.6
118	B78	MeOH	1.50	4	0.989	-9.80	5.72	0.25	99.4
119	B79	MeOH	1.39	5	0.961	-2.58	3.07	0.16	99.5

^a Stability constants given in Table IV. ^b Number of points used in the correlation. ^c Correlation coefficient. ^d Standard deviation of the estimate. ^e Confidence level. ^f Propylene carbonate.

^g *cis-syn-cis*. ^h +0.05 M Bu₄NClO₄. ⁱ 22°C. ^j +0.01 M Me₄NBr. ^k Correlated with R_m .

Table III. Radii of Alkali Metal Cations and Some Macrocycles

Cation	Radius (Å) ¹	Macrocycle	Radius (Å) ^{1,7,8}
Li ⁺	0.76	A1	0.86 - 0.92; 0.85 - 1.1
Na ⁺	1.02	A2	1.34 - 1.43; 1.3 - 1.6
K ⁺	1.38	A3	1.7; 1.7 - 2.1
Rb ⁺	1.52	A18	1.10
Cs ⁺	1.67	A19	1.40

Table IV. Stability Constants of 1:1 Complexes Formed between Alkali Metal Cations and Macrocycles at 25°C

No. ^a	Log K _a					Ref.
	Li ⁺	Na ⁺	K ⁺	Rb ⁺	Cs ⁺	
1	1.23	3.48	3.39		2.18	1 ^d
2		4.36	6.08	5.43	4.60	1
3	-0 ^b	0.8	2.03	1.56	0.99	1
4		2.76	4.33	3.46	2.84	1
5		5.46	6.28	5.32	4.5	1
6		2.13	4.32	4.86	5.01	1
7	0.6	1.21	2.02	1.52	1.25	1
8	5.28	6.36	8.30	6.71	6.26	9
9		1.42	2.08	1.53	0.9	1
10		4.29	5.1	4.86	3.88	1
11		5.3	5.4	4.5	3.6	1
12		4.9	5.3	4.4	3.8	1
13		4.90	5.30	4.40	4.05	1
14		4.4	5.0	4.23	3.55	1
15		2.1	4.60	4.6	4.2	1
16 ^c		3.60	4.80	4.90	3.80	1
17	2.00	3.23	5.04	4.82	4.70	10
18	2.00	3.04	4.56	4.28	4.16	10
19	2.40	3.20	5.04	4.85	4.70	10
20	2.60	3.41	5.12	4.87	4.74	10
21	3.00	3.20	4.08	3.74	3.52	10
22	4.32	6.08	7.91	7.04	6.08	11
23	4.36	6.23	7.63	5.67	5.76	9
24	4.34	5.22	6.23	5.27	4.71	12
25	5.38	9.48	8.54	6.74	4.33	1
26	9.6	12.8	9.9	7.0	4.9	1
27	6.97	10.7	10.5		4.55	1

Table IV. cont.

No. ^a	-----Log K _a -----					Ref.
	Li ⁺	Na ⁺	K ⁺	Rb ⁺	Cs ⁺	
28	7.33	12.98	11.22	9.31		13
29	2.6	7.9	10.6	8.98	4.4	1
30	1.25	4.0	5.3	4.06	1.44	1
31		10.56	13.20	12.32	7.55	13
32	2.0	7.0	9.42	7.61	3.21	1
33	2.19	7.50	9.21	7.19	2.98	1
34	2.2	7.5	8.7	5.91	2.61	1
35	4.18	6.24	5.28	4.65	4.38	14
36	4.18	5.18	7.24	≥6.42 ^b	5.59	14
37	3.49	3.85	4.91	5.14	4.81	14
38	3.63	4.40	6.06	5.47	4.72	14
39	≪ 2.40 ^b	3.34	4.10	3.93	3.92	14
40	< 2.0 ^b	3.5	5.2	3.4	2.7	1
41	4.30	5.95	6.09		5.68	2
42	4.00	4.67	6.26		5.06	2
43	2.93	3.30	3.59	3.38	3.28	12
44	2.75	3.70	3.94	3.77	3.79	12
45	4.21	6.09	6.57		5.75	2
46	4.11	4.63	5.98	5.99	5.98	2
47	3.34	3.90	4.61		4.40	2
48	3.85	4.19	5.37	5.35	5.30	2
49	3.69	4.49	5.02	4.94	5.35	2
50	5.11	8.96	8.66	7.66	6.57	15
51	5.04	8.79	8.30	6.96	5.69	15
52	4.78	5.80	5.86	4.99	4.79	15
53	5.41	8.79	7.98	6.60	5.72	15
54	5.51	9.15	9.45	8.34	6.60	15
55	4.96	6.51	7.48	6.15	5.40	15

Table IV. cont.

No. ^a	-Log K _a					Ref.
	Li ⁺	Na ⁺	K ⁺	Rb ⁺	Cs ⁺	
56	5.34	9.32	10.18	8.64	7.11	15
57	4.20	7.56	6.40	4.76	4.28	15
58	4.18	6.40	6.66	4.98	4.23	15
59	6.23	9.52	8.93	7.20	5.85	15
60	7.70	10.69	10.69	9.36	8.28	15
61	13.79	15.11	11.00	9.75	7.63	13
62	9.79	15.41	>14.57 ^b	14.96	12.01	13
63	7.26	9.90	13.93	14.89	15.91	13
64	9.08	9.41	9.00	8.79	8.57	11
65	8.86	11.28	11.43	10.40	9.59	11
66	8.86	10.04	10.18	8.64	7.69	11
67	13.40	11.94	9.08	8.34	8.64	16
68	12.15	11.28	7.91	6.89	7.69	16
69	8.79	10.62	11.15	9.45	8.41	16
70	9.23	12.08	10.52	10.48	9.08	16
71	7.84	9.45	8.79	7.61	7.18	16
72	5.57	8.86	7.61	6.00	5.41	16
73	8.11	11.64	9.59	7.91	7.98	16
74	8.86	11.20	11.34	10.15	9.59	16
75	4.40	4.32	5.28	5.43	5.79	17
76	5.51	6.38	7.34	6.60	6.15	17
77	5.30	9.90	7.84	6.20	5.20	18
78	5.23	9.61	8.04	6.83	5.95	18
79	5.20	9.20	8.62	7.60	6.53	18
80	4.26	7.00	5.15	4.52	4.23	18
81	4.61	9.00	7.67	6.52	5.57	18
82	5.08	5.15	5.74	4.51	4.40	18

Table IV. cont.

No. ^a	Log K_a					Ref.
	Li ⁺	Na ⁺	K ⁺	Rb ⁺	Cs ⁺	
83	4.08	4.15	4.70	4.40	4.34	18
84	4.23	5.45	6.18	4.99	4.58	18
85	4.85	7.18	8.20	7.49	6.46	18
86	4.38	5.04	6.43	5.93	5.26	18
87	4.18	6.54	8.15	8.18	8.08	18
88	4.74	5.15	7.81	8.04	7.88	18
89	6.41	6.76	8.88	8.96	8.04	18
90	4.76	5.20	8.51	8.36	7.62	18
91	5.34	5.91	7.00	7.32	7.08	18
92	4.45	4.89	6.81	6.74	6.20	18
93	4.53	5.82	6.18	5.77	5.45	18
94	4.04	6.20	6.76	6.08	5.20	18
95	5.34	7.99	7.48	6.26	5.26	18
96	4.77	4.92	6.11	5.86	5.72	18
97	4.11	7.40	7.48	5.64	4.04	19
98	<4.40 ^b	5.86	7.40	6.74	5.34	19
99	4.11	6.38	7.48	6.15	4.54	19
100	6.00	8.56	8.95	8.04	7.32	20
101	6.28	9.80	9.08	7.92	7.90	20
102	4.89	7.34	7.63	7.11	6.65	20
103	5.46	7.23	6.89	6.15	5.94	20
104	6.04	7.88	7.54	6.95	6.62	20
105	8.95	11.08	11.32	9.28	8.69	9
106	3.58	4.15	4.32		3.70	12
107	3.46	4.66	5.26		5.81	12
108	4.76	6.39	7.20	6.28	5.71	12
109		3.79	3.38	2.91	2.85	12
110	2.91	5.69	4.82	3.94	3.94	12

Table IV. cont.

No. ^a	Log K _a					Ref.
	Li ⁺	Na ⁺	K ⁺	Rb ⁺	Cs ⁺	
111	5.01	7.69	8.52	6.28	5.49	12
112	4.11	4.52	5.36	5.29	5.56	2
113	12.67	14.28	12.15	11.15	10.76	21
114	11.57	13.99	10.04	9.15	8.86	21
115	11.79	11.15	8.49	7.98	7.76	21
116	7.61	7.48	9.08	8.49	8.41	21
117	9.96	12.23	11.49	10.84	10.62	11
119		0.88	4.7	5.19	4.36	1
120	1.28	2.4	2.92	2.74	2.34	1

^a The numbering corresponds to that in Table II. ^b Not used in the correlation

because of uncertainty in the value. ^c 22°C. ^d Average log K_a value is used

whenever more than one value is listed in all the data taken from ref. 1.

The macrocycles are divided into two groups: (1) the ligating atoms are part of the macrocyclic ring structure (A1 to A28); (2) some or all of the ligating atoms are not part of the macrocyclic ring structure (B1 to B79). The first group of macrocycles give good correlations (Table I). There is not a single correlation (out of a total of forty) with a correlation coefficient $r < 0.90$ and a confidence level less than 95%. Some of the macrocycles in the second group have methyl substituents attached to their ligating atoms. These methyl groups may give rise to steric hindrance if they point into the cavity and resulting in poorer correlations. However, the results (Table I) show that steric effect is probably not serious because, on the whole, good correlations are still obtained. Only six correlations have $r < 0.90$ (no. 80, 82, 101, 110, 116 and 117) and two with a confidence level less than 95% (no. 82, 116). It is difficult to state with certainty the reason(s) for these few poorer correlations. Steric factor is unlikely to be the reason for the poor correlation obtained for no. 82 (Table II) since the macrocycle B42 is very similar to B43 which gives a satisfactory correlation in no. 83. Sometimes the accuracy of the experimental log K_a values could be a contributing factor. For example, the earlier log K_a value for Rb⁺ in no. 43 was given by Cram and coworkers² as 3.23 instead of their more recent value of 3.38 (Table IV, no. 43). If the earlier log K_a value for Rb⁺ were used, a poorer correlation for no. 43 is obtained ($R_c = 1.33$ Å, $n = 5$, $r = 0.921$, $m = -1.12$, $b = 3.59$, $S_d = 0.08$ and confidence level = 98.5%).

Table V. Comparison of Observed^a and Calculated^b Log K_a Values for the NH_4^+ Complexes

No. ^c	Log K_a	No. ^c	Log K_a	No. ^c	Log K_a	No. ^c	Log K_a
1	3.03(3.41) ^d	43	3.28(3.53)	67	8.64(9.34)	92	6.36(6.87)
2	4.20(5.84)	44	3.93(4.15)	68	7.61(8.24)	93	5.71(6.35)
3	1.16(1.86)	45	5.90(7.33)	69	9.74(10.4)	94	5.70(7.03)
6	3.27(4.45)	46	5.68(6.20)	70	10.5(10.8)	95	6.38(7.17)
7	0.8(1.83)	47	3.77(4.74)	71	7.54(8.62)	96	5.48(6.07)
8	7.83(7.63)	48	4.85(5.26)	72	6.30(7.24)	97	4.98(6.90)
15	2.4(4.80)	49	4.71(4.96)	73	8.04(9.34)	98	6.08(7.16)
17	5.06(5.16)	50	7.18(8.59)	74	10.5(11.1)	99	5.49(6.95)
18	4.60(4.71)	51	6.54(7.94)	75	5.87(5.31)	100	7.52(8.80)
19	5.08(5.11)	52	4.69(5.58)	76	6.15(7.05)	102	6.61(8.09)
20	5.09(5.21)	53	6.34(7.71)	77	6.36(7.61)	103	6.67(6.76)
21	4.03(3.92)	54	7.54(9.22)	78	6.74(8.06)	104	6.96(7.48)
22	6.96(7.62)	55	6.00(6.95)	79	7.36(8.56)	105	9.99(10.6)
23	6.51(6.99)	56	8.11(9.84)	81	6.64(7.69)	106	3.62(4.26)
24	5.50(5.82)	57	4.88(6.07)	83	4.20(4.56)	107	5.11(5.53)
31	12.6(14.9)	58	4.88(6.10)	84	5.46(5.74)	108	5.78(6.94)
35	4.38(4.01)	59	6.74(8.37)	85	7.26(8.50)	109	3.28(3.22)
36	6.65(6.87)	60	9.30(10.4)	86	6.40(6.19)	111	6.43(7.75)
37	5.25(4.98)	62	13.6(16.9)	87	7.82(8.52)	112	5.06(5.27)
38	5.71(5.78)	63	14.8(13.9)	88	7.53(7.70)	113	10.9(11.9)
39	3.96(4.15)	64	8.79(8.89)	89	8.04(8.94)	114	9.74(10.3)
41	5.70(5.79)	65	10.5(11.2)	90	7.88(8.42)	115	8.04(8.68)
42	5.56(6.05)	66	9.23(9.46)	91	6.80(7.09)	118	1.67(5.03)
						119	1.92(2.97)

^a The references are given in Table IV. ^b Using the correlation lines given in Table II;

the R_m value for NH_4^+ is 1.43 Å (ref. 22). ^c The numbering corresponds to that in

Table II. ^d Calculated values in parentheses.

Steric factor is expected to be significant in the case of the functionalized calixarenes (C1 - C5) since some of the flexible chains attached to the ligating oxygen atoms point into the cavity defined by the ligating oxygen atoms.^{3,4} The reported log K_a data⁵ of these macrocycles are poorly correlated by equation 1.

When the cavity size adopted by the macrocycle for complexation is larger than the size of the largest alkali metal cation Cs^+ and the first assumption given earlier is still valid, the correlation equation becomes

$$\log K_a = mR_m + b \quad (2)$$

Three of the complexation equilibria (no. 49, 63 and 75) are better correlated by equation 2.

The NH_4^+ cation is not included in the correlation because, unlike the alkali metal cations, it uses four hydrogen atoms instead of the central charged nitrogen atom to coordinate to its ligating atoms. The log K_a values for the NH_4^+ complexes calculated from the correlation lines in Table II are given in Table V. The differences between the observed and calculated values are higher than the standard deviations of the estimate in Table II.

The other two metal cations, Ag^+ and Tl^+ , are also not included in the correlations because they are soft cations, unlike the alkali metal cations which are hard.⁶ They generally deviate from the correlation lines of the alkali metal cations, as shown by a comparison of their observed and calculated log K_a values (Table VI).

Table VI. Comparison of Observed^a and Calculated^b Log K_a Values for Ag^+ and Tl^+ Complexes

No. ^c	Log K_a (Ag^+)	Log K_a (Tl^+)	No. ^c	Log K_a (Ag^+)	Log K_a (Tl^+)
1	3.62(3.89) ^d	4.6; 5.26(5.48)	14	4.04(5.05)	3.86(4.38)
2	4.58(5.02)		15	4.45(4.99)	2.4(4.80)
3	1.55(1.28)	2.27(1.61)	25	14.0(11.3)	
5	7.10(6.29)	7.13(5.49)	26	18.6(12.7)	
6	2.46(2.89)		27	8.9(13.4)	12.3(7.93)
7	1.7(1.57)	1.8(1.65)	29	12.1(10.8)	10.1(8.4)
10		4.60(4.93)	33	11.8(10.5)	7.9(6.9)
13		5.70(4.74)	118	3.90(2.29)	4.06(5.72)

^a The references are given in Table IV. ^b Using the correlation lines given in Table II; the R_m values for Ag^+ and Tl^+ are 1.15 and 1.50 Å respectively.¹ ^c The numbering corresponds to that in Table II. ^d Calculated values in parentheses.

Conclusion. The stability constants of 1:1 complexes formed between alkali metal cations and macrocycles are satisfactorily correlated by equation 1 when the macrocycles do not have flexible chains that will interfere with their cavity size defined by the ligating atoms.

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